

Folien zur Vorlesung am 8.04.2025
3D Computer Vision

PERSPEKTIVEN UND ANWENDUNGEN

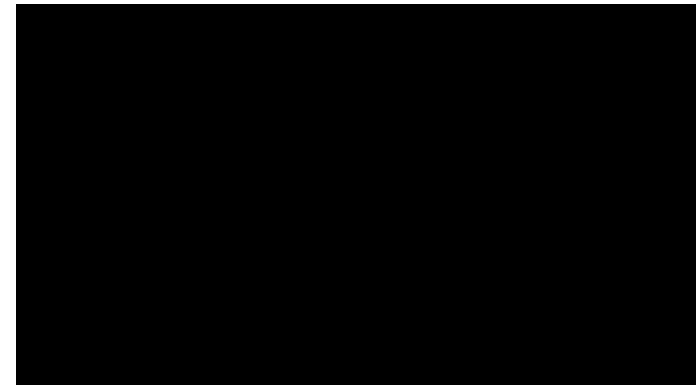
Ames Room



Task:
Draw this room as
seen from the top
and the side.

[3DCV Youtube Playlist \(Ames Window + Die Ärzte\)](#)

Forced perspective in film



https://www.youtube.com/watch?v=QWMFpxkGO_s

3D to 2D: perspective projection

Projection:

$$\mathbf{p} = \begin{bmatrix} wx \\ wy \\ w \end{bmatrix} = \begin{bmatrix} * & * & * & * \\ * & * & * & * \\ * & * & * & * \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix} = \mathbf{\Pi P}$$

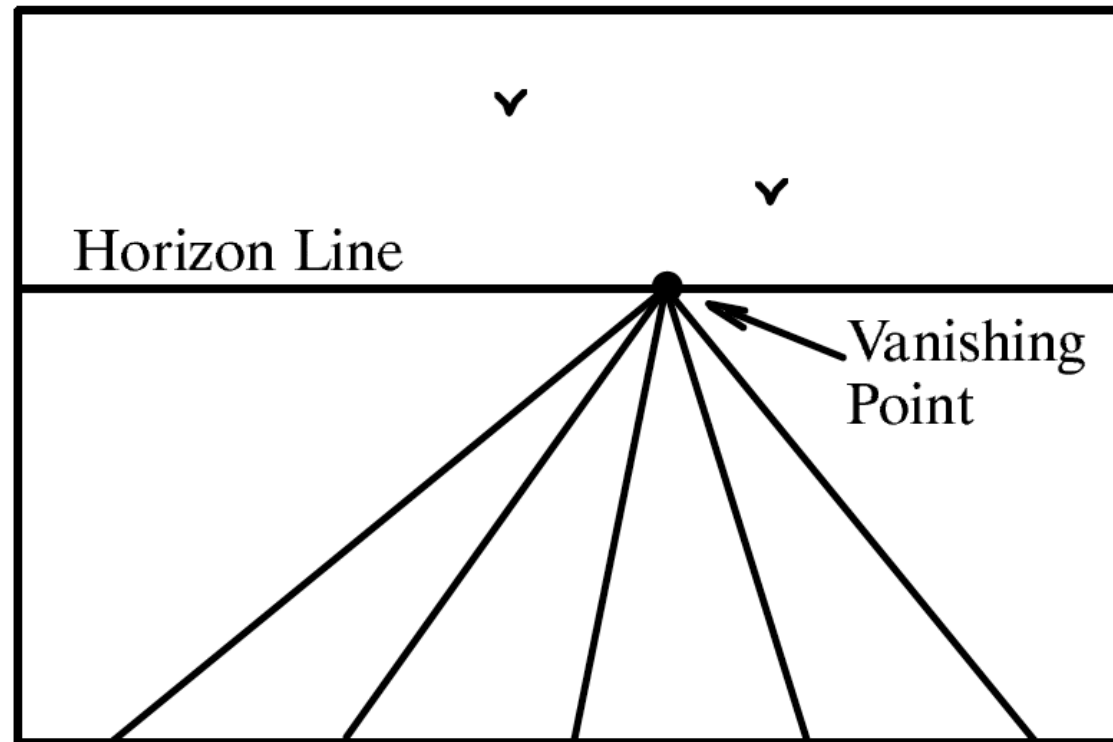
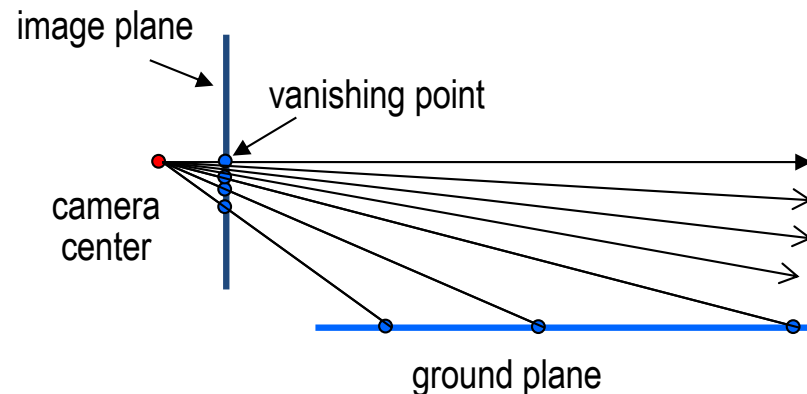


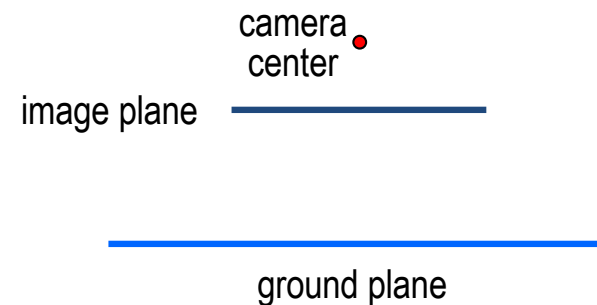
Figure 23.4

A perspective view of a set of parallel lines in the plane. All of the lines converge to a single vanishing point.

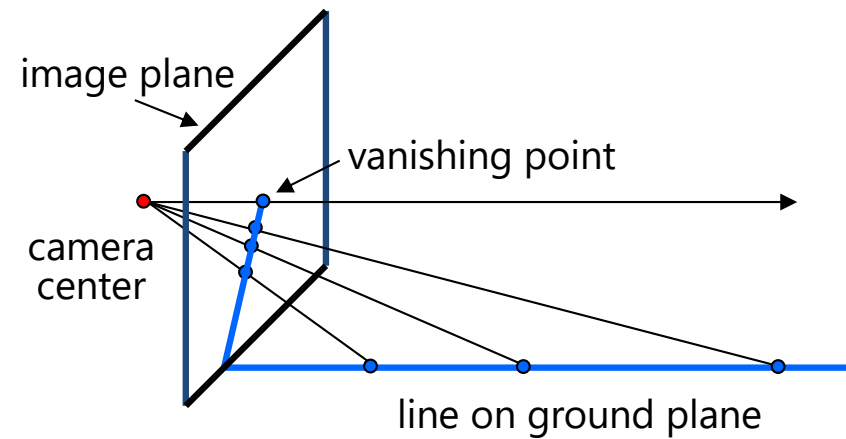
Vanishing points (1D)



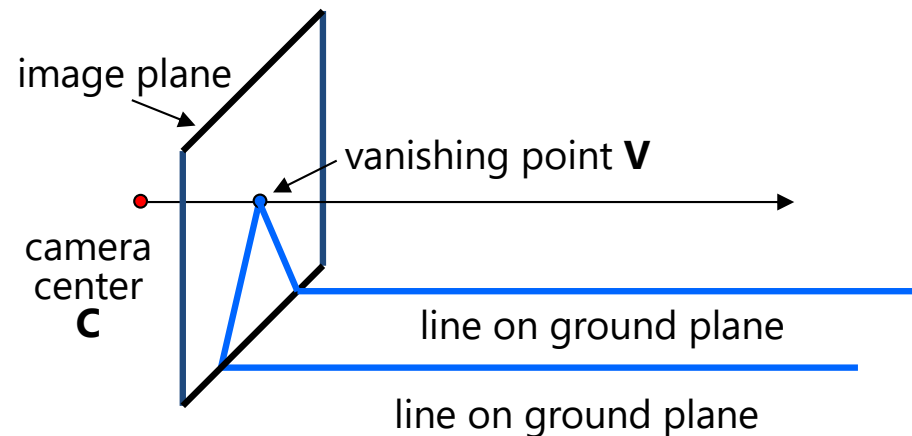
- Vanishing point
 - projection of a point at infinity
 - can often (but not always) project to a finite point in the image



Vanishing points (2D)



Vanishing points

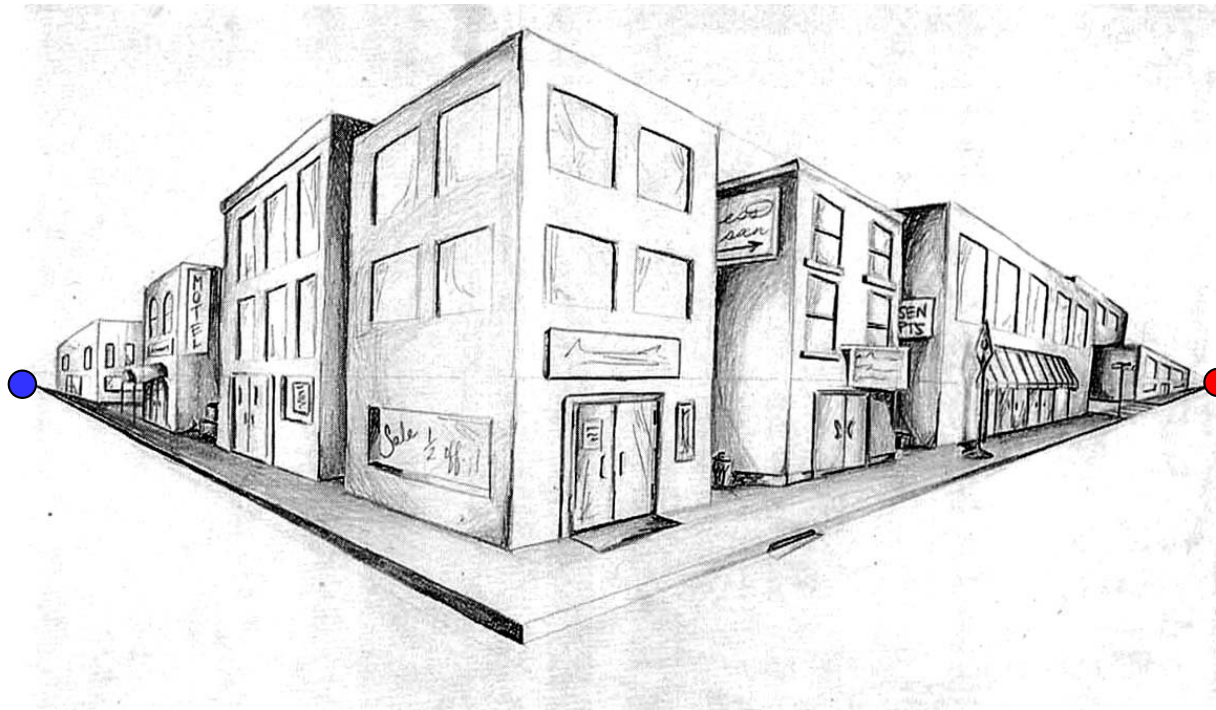


- Properties
 - Any two parallel lines (in 3D) have the same vanishing point $\mathbf{v}$
 - The ray from $\mathbf{C}$ through $\mathbf{v}$ is parallel to the lines
 - An image may have more than one vanishing point
 - in fact, every image point is a potential vanishing point

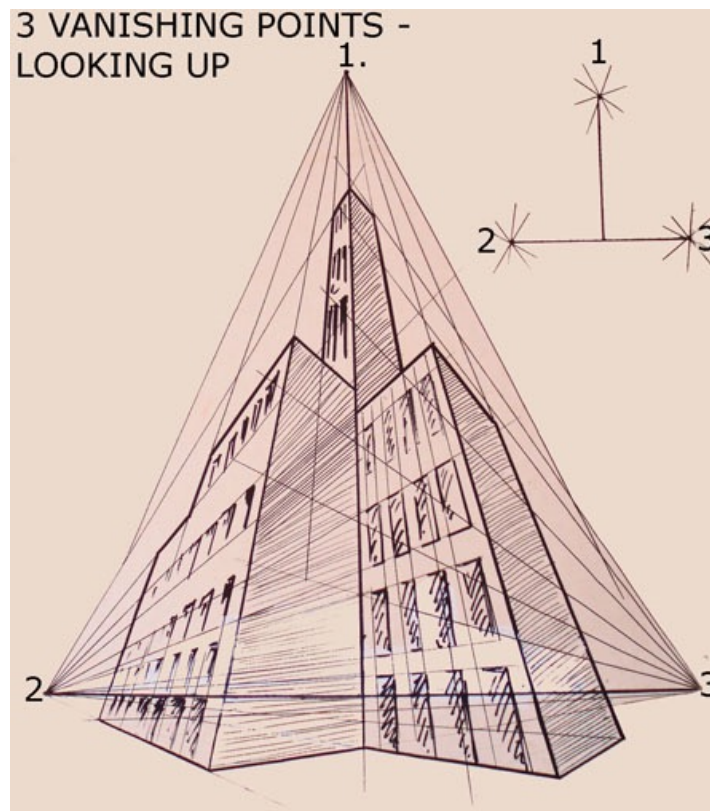
One-point perspective



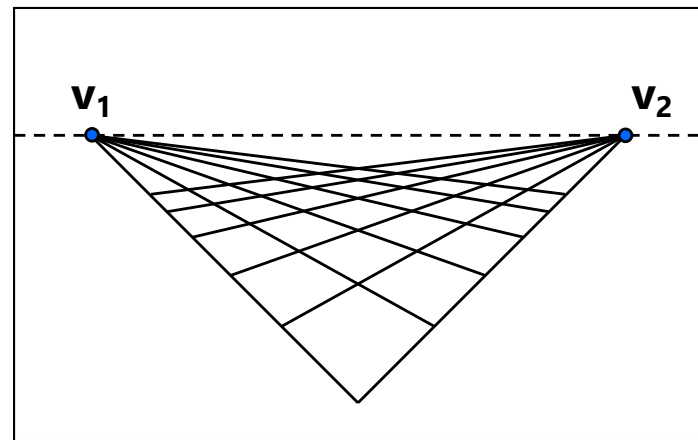
Two-point perspective



Three-point perspective

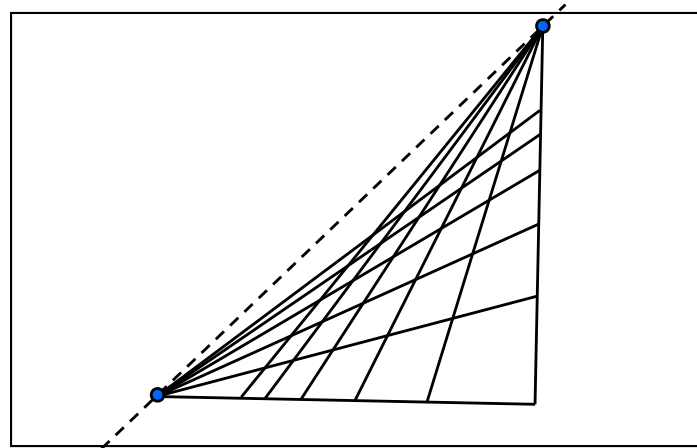


Vanishing lines



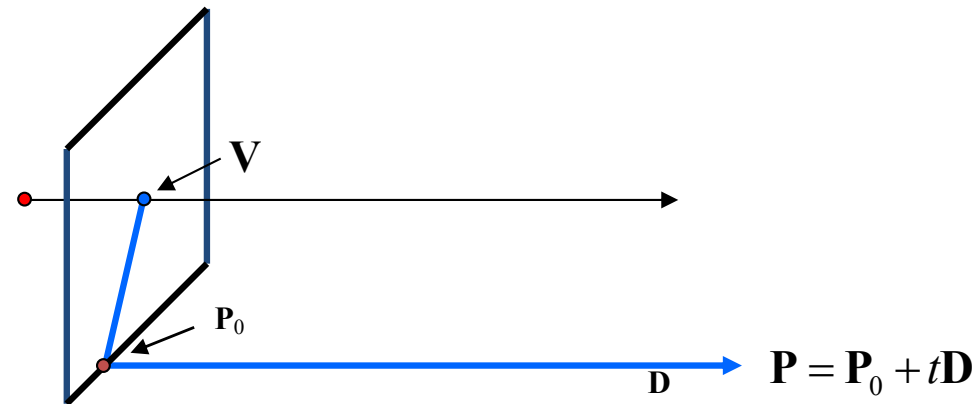
- Multiple Vanishing Points
 - Any set of parallel lines on the plane define a vanishing point
 - The union of all of these vanishing points is the *horizon line*
 - also called *vanishing line*
 - Note that different planes (can) define different vanishing lines

Vanishing lines

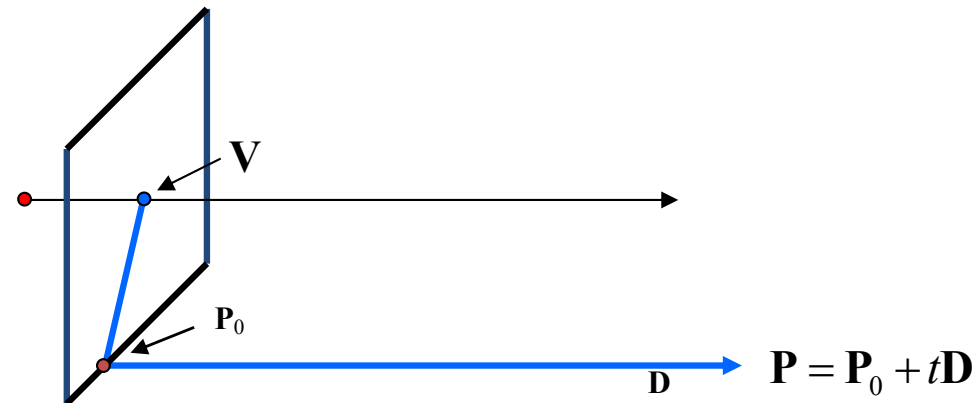


- Multiple Vanishing Points
 - Any set of parallel lines on the plane define a vanishing point
 - The union of all of these vanishing points is the *horizon line*
 - also called *vanishing line*
 - Note that different planes (can) define different vanishing lines

Computing vanishing points



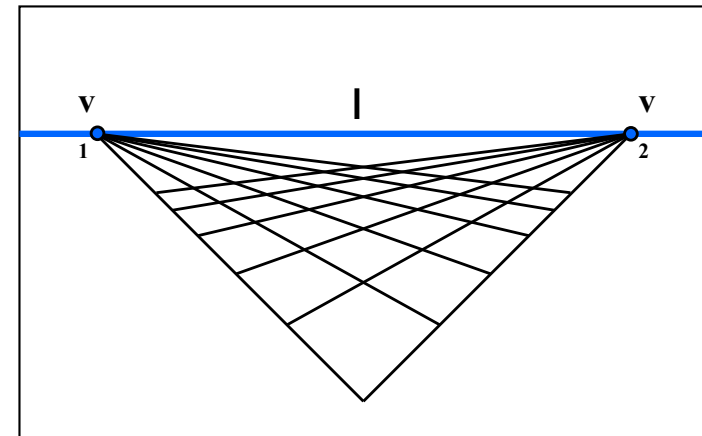
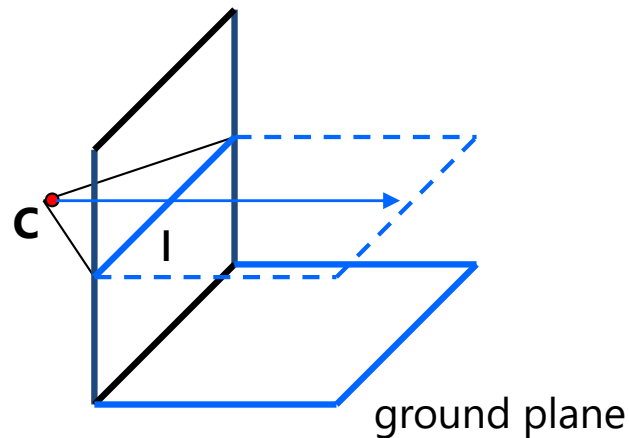
Computing vanishing points



$$\mathbf{P}_t = \begin{bmatrix} P_X + tD_X \\ P_Y + tD_Y \\ P_Z + tD_Z \\ 1 \end{bmatrix} \cong \begin{bmatrix} P_X / t + D_X \\ P_Y / t + D_Y \\ P_Z / t + D_Z \\ 1/t \end{bmatrix}$$

- Properties $\mathbf{v} = \mathbf{I}\mathbf{P}_\infty$
 - $\mathbf{P}_\infty$ is a point at *infinity*, $\mathbf{v}$ is its projection
 - Depends only on line *direction*
 - Parallel lines $\mathbf{P}_0 + t\mathbf{D}$, $\mathbf{P}_1 + t\mathbf{D}$ intersect at $\mathbf{P}_\infty$

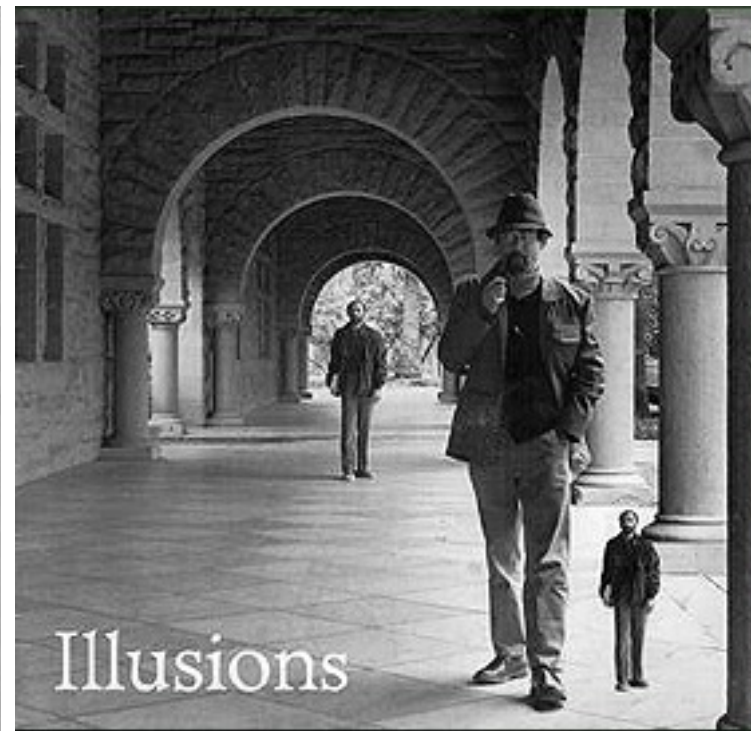
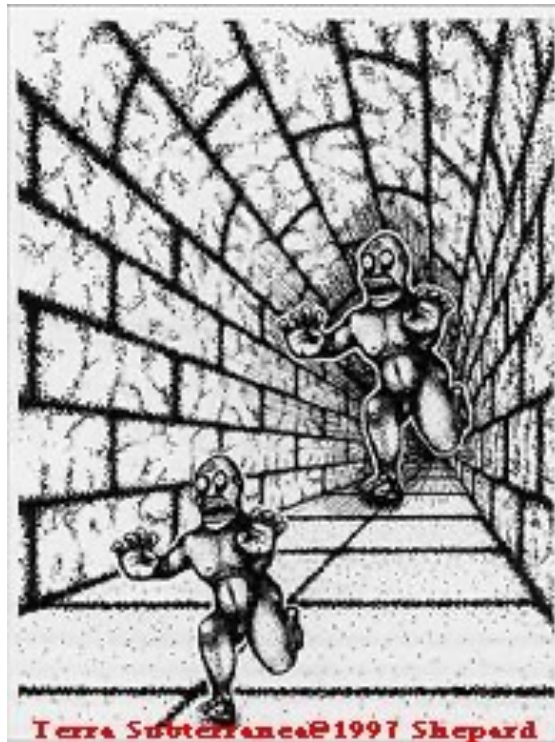
Computing vanishing lines



- Properties
 - l is intersection of horizontal plane through C with image plane
 - Compute l from two sets of parallel lines on ground plane
 - All points at same height as C project to l
 - points higher than C project above l
 - Provides way of comparing height of objects in the scene



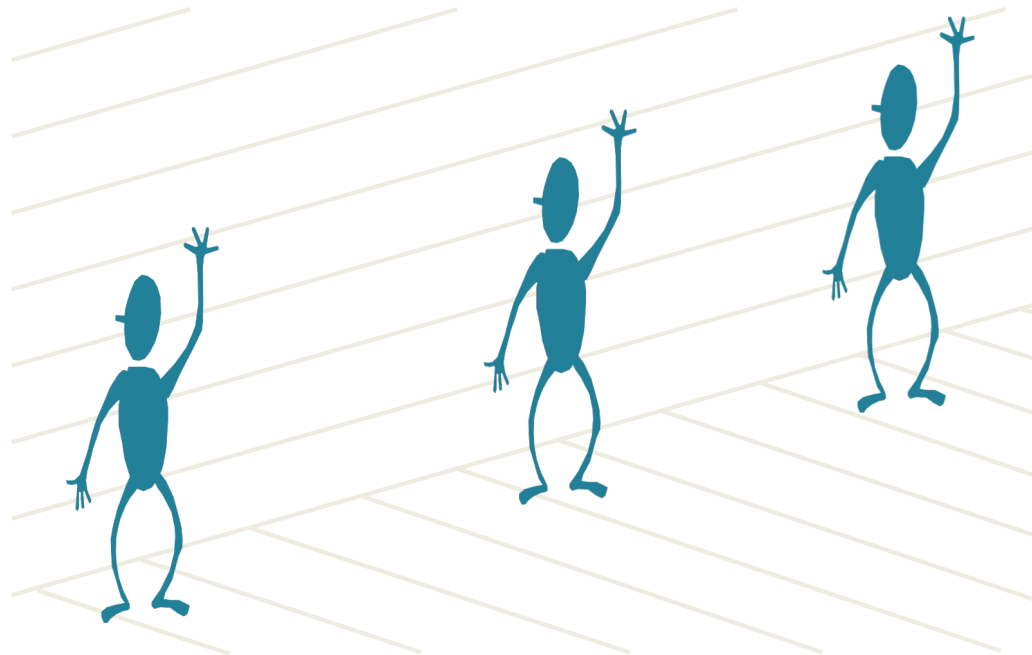
Fun with vanishing points



Lots of fun with vanishing points



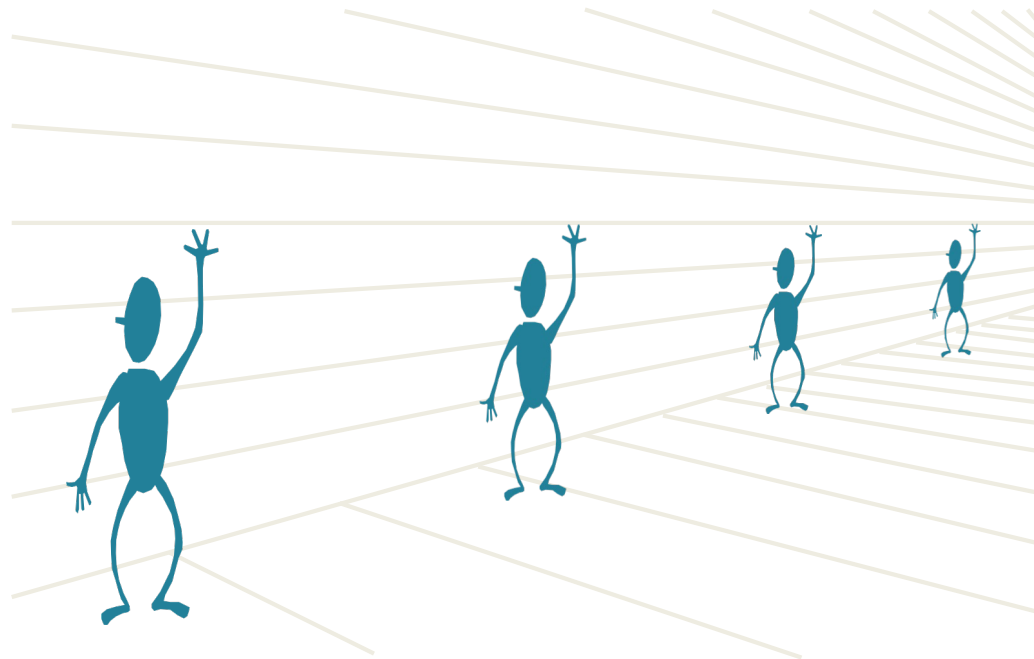
Perspective cues



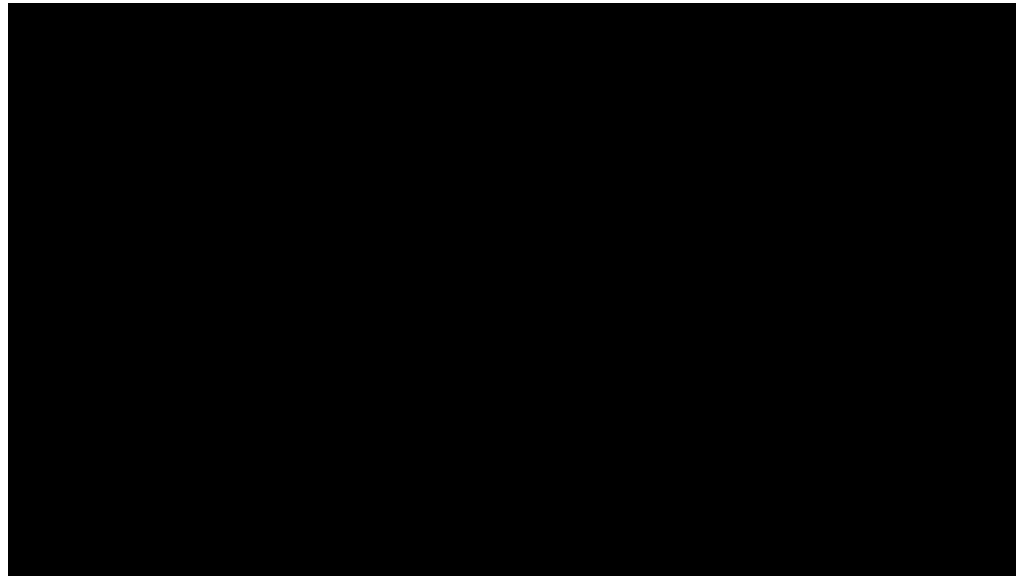
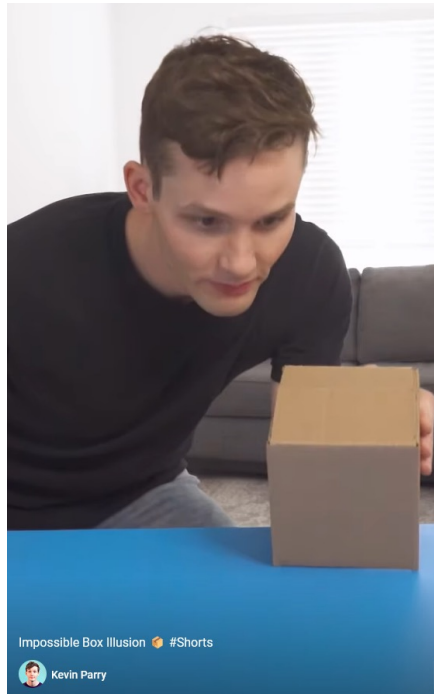
Perspective cues



Perspective cues



More fun with perspectives



https://www.youtube.com/shorts/xq_CmZ3d6pk